

Honors Geometry

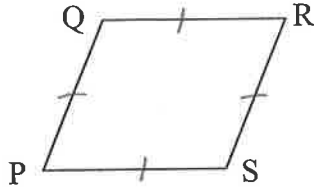
Section 6.4 Notes

Properties of Rhombuses, Rectangles and Squares

Name: Key

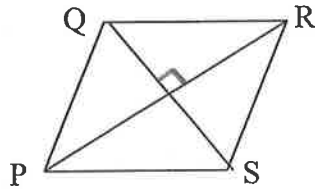
****All of these shapes are special types of parallelograms and therefore have the same properties as parallelograms. REFER TO YOUR CHART!!**

A **Rhombus** is a parallelogram with four congruent sides.



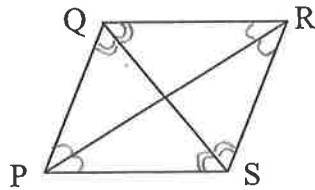
$$\overline{PQ} \cong \overline{QR} \cong \overline{RS} \cong \overline{SP}$$

A **Rhombus** is a parallelogram in which its diagonals are perpendicular.



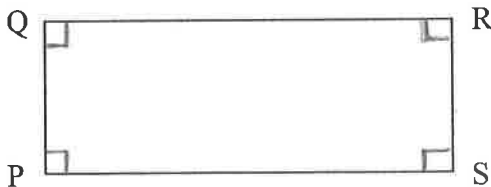
$$\overline{QS} \perp \overline{PR}$$

A **Rhombus** is a parallelogram in which its diagonals bisect each pair of opposite angles.



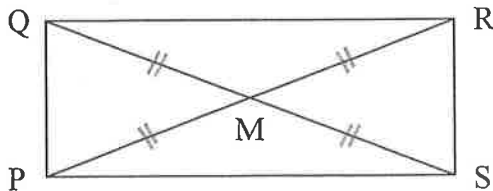
$$\begin{aligned} \overline{QS} &\text{ bisects } \angle PQR \text{ and } \angle PSR \\ \overline{PR} &\text{ bisects } \angle QPS \text{ and } \angle QRS \end{aligned}$$

A **Rectangle** is a parallelogram with four right angles.



$$\angle P, \angle Q, \angle R, \angle S \text{ are right angles}$$

A **Rectangle** is a parallelogram in which its diagonals are congruent.

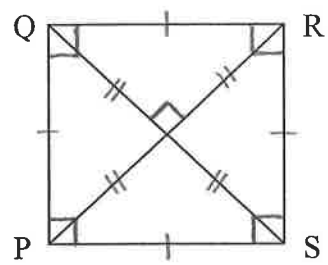


$$\overline{QS} \cong \overline{PR}$$

$$\overline{QM} \cong \overline{MR} \cong \overline{PM} \cong \overline{MS}$$

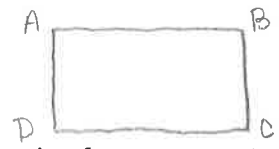
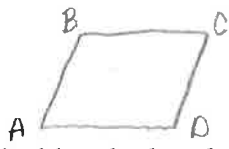
* What kind of triangles are formed ?

A **Square** has the properties of both rhombus and rectangles.



*All of these properties prove that all squares consist of 45-45-90 triangles.

Practice Problems



For any rhombus ABCD, decide whether the statement is *always*, *sometimes* or *never* true. Explain why.

<p>1. $\angle B \cong \angle D$</p> <p>Always</p> <p>- Opposite angles are congruent.</p>	<p>2. $\angle D$ is right</p> <p>Sometimes</p> <p>- Only if the rhombus is a square.</p>	<p>3. $\overline{AC} \cong \overline{BD}$</p> <p>Sometimes</p> <p>- Only if the rhombus is a square.</p>
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For any rectangle ABCD, decided whether the statement is *always*, *sometimes* or *never* true. Explain why.

<p>1. $\angle A \cong \angle B \cong \angle C \cong \angle D$</p> <p>Always</p> <p>- All angles are 90°.</p>	<p>2. $\overline{AC} \perp \overline{BD}$</p> <p>Sometimes</p> <p>- Only if rectangle is a square.</p>	<p>3. $\overline{AC} \cong \overline{BD}$</p> <p>Always</p> <p>- Diagonals are congruent.</p>
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The diagonals of rhombus EFGH intersect at J. Given that $FJ = 10$ and $m\angle HGE = 42^\circ$, find the indicated measures.

1. $m\angle FGE$

(42°)

2. FH

(20)

3. $m\angle HEG$

(42°)

4. $m\angle EHJ$

$180 - 90 - 42$

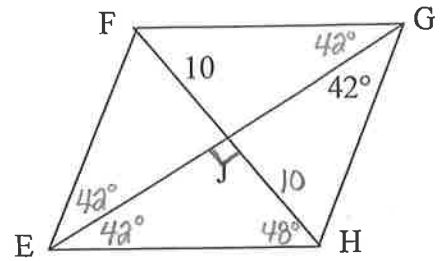
(48°)

5. $m\angle FJE$

(90°)

6. $m\angle GFJ$

(48°)



The diagonals of rectangle ABCD intersect at E. Given that $AC = 16$ and $m\angle ABD = 28^\circ$, find the indicated measures.

1. $m\angle CBD$

$90 - 28$

(62°)

2. BD

(16)

3. $m\angle BEC$

$180 - 62 - 62$

(56°)

4. AE

(8)

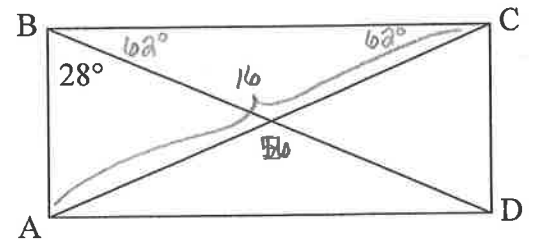
5. $m\angle CED$

$180 - 56$

(124°)

6. ED

(8)



* not drawn to scale

The diagonals of square QRST intersect at V. Given that $QV = 4$, find the indicated measures.

1. $m\angle QRT$

(45°)

2. RT

(8)

3. $m\angle SVT$

(90°)

4. VS

(4)

5. $m\angle RSQ$

(45°)

6. RV

(4)

